

# Generating Complex Metamorphic Relations for Cyber-Physical Systems with Genetic Programming

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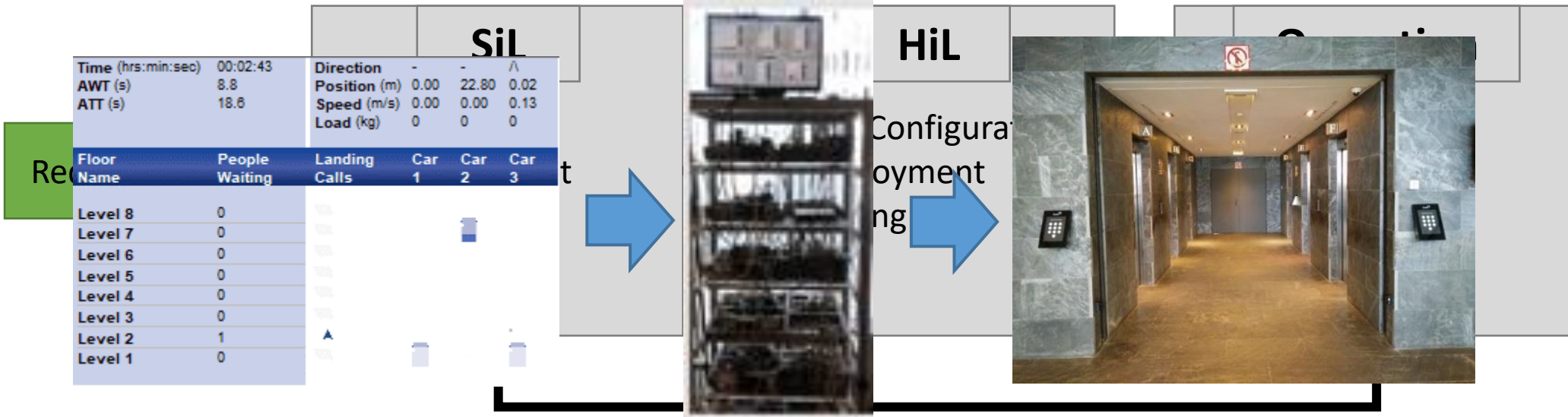
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- Leading elevator company in Europe
- Design, manufacturing, installation and maintenance of:
  - Elevators
  - Escalators
  - Moving ramps
  - ...
- Multi-elevator installations



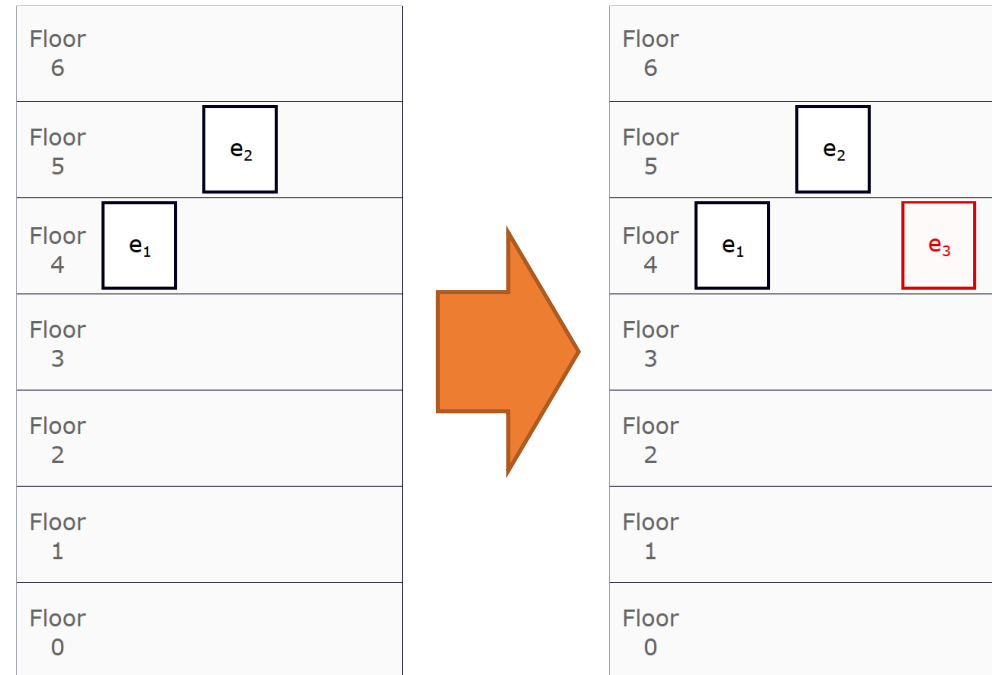
# Software maintenance process



- New releases take an average of around **a year to complete this process**
- Many of these steps are **not fully automated**
- Notably, major reliance on **human test oracles**

# Metamorphic Testing

- Based on the relations among the inputs and outputs of **two or more test executions**, the so called metamorphic relations (MRs)
- MRs for the domain of elevation already defined in our previous work [1]



$$E_f = E_s \cup E' \Rightarrow AWT_f < AWT_s$$

[1] Ayerdi et al. QoS-aware Metamorphic Testing: An Elevation Case Study. ISSRE 2020.

# Automatic generation of MRs

- MRs have been proven effective
- Manual definition of MRs can be **costly and error-prone**
  - Requires in-depth knowledge of the domain and the system
- Build on top of GAssert, a technique for **automatically generating** and improving **program assertions** [1]

**GAssertMRs, Genetic ASSERTion improvement for MRs [2]**

[1] Terragni et al. Improving Assertion Oracles with Evolutionary Computation. ESEC/FSE 2020.

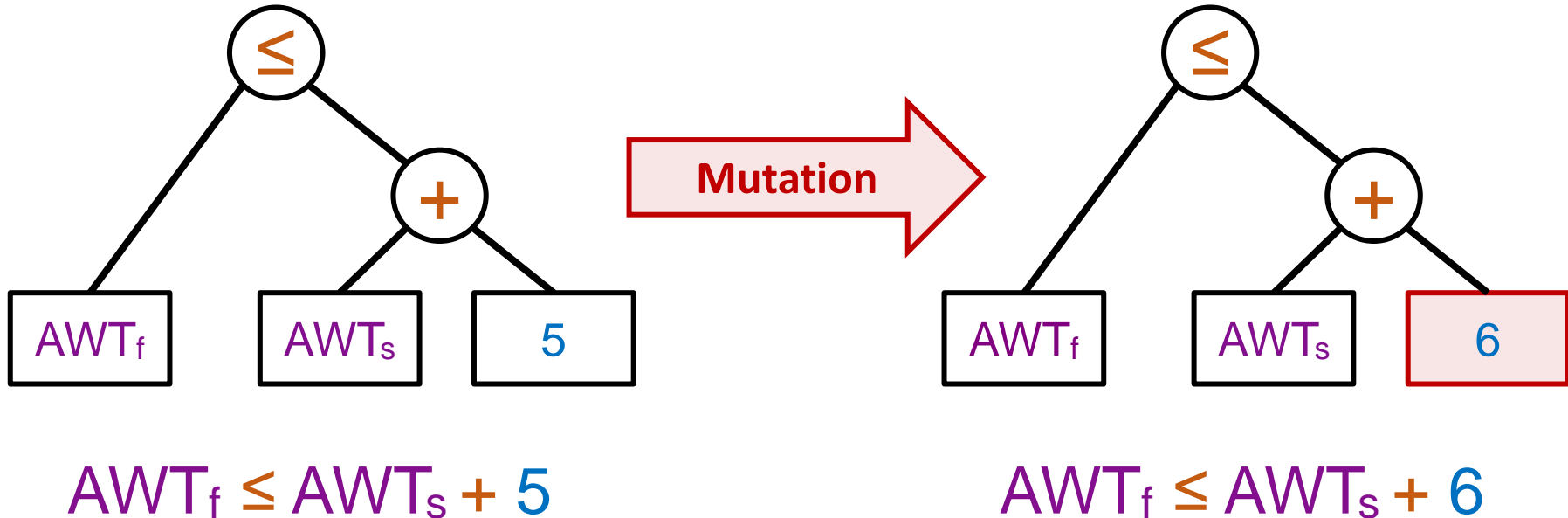
[2] Ayerdi et al. Generating Metamorphic Relations for Cyber-Physical Systems with Genetic Programming: an Industrial Case Study. ESEC/FSE 2021.

# Evolutionary Algorithm

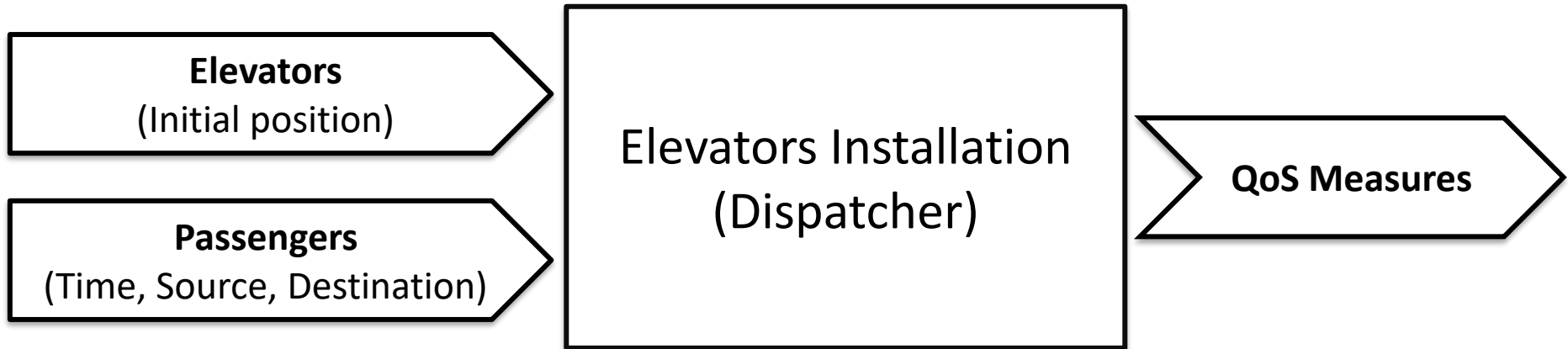
- Fitness for MRs: Minimize **FPS**, **FNS** and **complexity**
  - Usually evaluated with **mutation testing**
  - Real failures could be used if available
- Template for performance/QoS related MRs:
  - $\langle \text{METRIC}_f \rangle \langle \text{operator} \rangle \langle \text{expression} \rangle$
  - $\text{AWT}_f \leq \text{AWT}_s + 5$
- Only the  $\langle \text{expression} \rangle$  part is generated by GAssertMRs
  - Reduced **search space**
  - MRs are **easier to understand** by humans

# Genetic Programming

- Individuals represented as expression trees
- Expressions can contain operators, variables and constants
  - Operators: Arithmetic (+, /, ...), relational (<, =, ...) or logical (AND, OR, ...)
  - Variables: System inputs or outputs
  - Constants: Numeric (-100, 100) or Boolean (true/false)



# Evaluation – Elevator Installations (Orona)

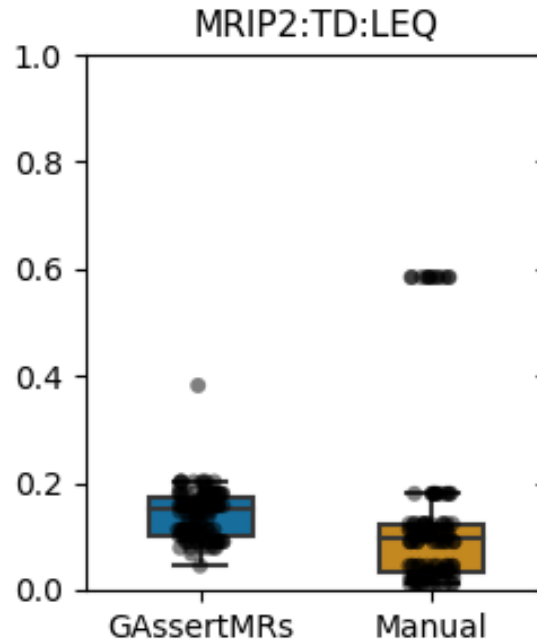


- QoS metrics
  - Average Waiting Time (AWT)
  - Total Distance (TD)
  - Total Movements (TM)
- Evaluation
  - Configurations: Try every QoS metric and operator (> or <) combination
  - **Learning** process took **15 mins** for each configuration

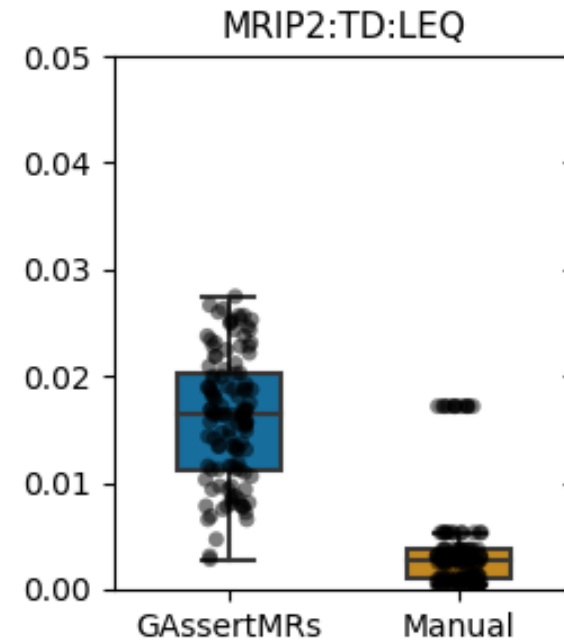


# Evaluation – Experimental Results

- GAssertMRs results in **almost zero FPs**
- **Outperforms manual MRs** in several configurations
- **Outperforms regular assertions** except for one configuration



Mutation Score



Failure Detection Ratio

# Future Extension – Complex Types

- Use **functional programming techniques** to enable the manipulation of collections
  - Function literals
  - Higher order functions

positionsDistance( $E_s$ ,  $E_f$ )



`sum(map([(es, ef)]{abs(es - ef)}, zip( $E_s$ ,  $E_f$ )))`

Floor 6		
Floor 5	e <sub>1</sub>	e <sub>2</sub>
Floor 4	e <sub>1</sub>	
Floor 3		
Floor 2		e <sub>2</sub>
Floor 1		
Floor 0		

$[(5,4), (5,2)] \rightarrow [1,3] \rightarrow 4$



**Mondragon  
Unibertsitatea**

Faculty of  
Engineering

Thank you

**Jon Ayerdi**

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